Spatial distribution of surface ablation in the terminus of Rhonegletscher, Switzerland

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ABSTRACT. The spatial pattern of glacier surface melt was measured with a resolution of 20–100 m within a region extending 1 km up-glacier from the terminus of Rhonegletscher, Switzerland. The melt rate was monitored from 6 July to 6 September 2009 using 44 ablation stakes. We also measured the surface albedo near the stakes to investigate the importance of this parameter for the melt-rate distribution. The melt rate varied from 32.8 to 71.9 mm w.e. d^{-1} in the study area. Our measurements suggest that the spatial variation of the melt rate can be explained by (1) shading of the ice surface by neighbouring mountains, (2) surface albedo and (3) effects of microclimate (e.g. radiation from side-walls) on the surface energy balance. The observed melt-rate distribution was compared to the results of a temperature-index melt model, which takes into account shading of direct solar illumination but not the other two effects. The model reproduces some important features of the field data, but its spatial variations are generally less than the measured values. Our study shows the importance of albedo and other local conditions in the accurate estimation of the small-scale melt-rate distribution.

INTRODUCTION

Glacier melt plays a key role in the hydrology of glacierized catchments. Run-off from mountain glaciers is an important resource for irrigation, hydropower generation and potable water in mountainous regions (e.g. Schaefli and others, 2007; Huss and others, 2008b). Accurate quantification of snow and ice melt on glaciers is therefore crucial for human activities. Melting is also important for the mass balance of mountain glaciers. Glaciers change their volume under the influence of climate conditions (e.g. Huss and others, 2009), and their mass loss significantly contributes to changes in global sea level (e.g. Meier and others, 2007). To predict future glacier evolution and its impact on human society, we must be able to estimate their melt rates from projected climate variables.

Glacier melt can be computed by energy-balance models (e.g. Klok and Oerlemans, 2002; Hock and Holmgren, 2005; Arnold and others, 2006). Solving the energy balance of the glacier surface involves the capture of complex processes, but such models require field observations that are difficult to acquire. Alternatively, glacier melt is often computed from air-temperature records by using temperature-index melt models (e.g. Braithwaite, 1995; Ohmura, 2001; Hock, 2003; Shea and others, 2009). Taking into account the expected spatial distribution of solar radiation improves computations of temporal and spatial glacier melt patterns (e.g. Hock, 1999). Such models have been tested against glacier discharge data, but their ability to reproduce small-scale spatial melt variation has not been well studied because high-resolution field data are lacking. Distributed temperature-index melt models do include some geometrical effects which determine the amount of potential solar radiation, such as shading by surrounding mountains and the angle of incidence of the solar beam on the glacier surface. Other key variables such as ice-surface albedo and

wind-mediated sensible and latent heat exchanges are more difficult to take into account, but are equally important. Albedo is particularly important on mountain glaciers (e.g. Oerlemans and others, 2009), but its spatial and temporal variability is difficult to model; it must be measured on the glacier (e.g. Brock and others, 2000) or by using satellite data (e.g. Klok and others, 2003).

To study spatial variations in glacier surface melt on the scale of tens of metres in the crucial region of a glacier terminus, we carried out field measurements on the terminus of Rhonegletscher, Switzerland. This paper reports surface melt rate and albedo measurements from July to September 2009. Both variables varied substantially over the studied area. The field data were compared with a distributed temperature-index melt model to evaluate the ability of the latter to reproduce small-scale melt patterns. The small-scale melt pattern is especially important for Rhonegletscher, which is rapidly thinning under the influence of factors related to proglacial lake formation. The non-uniform melt rates on the surface of the glacier control the evolution of the terminus and future development of the lake.

METHOD

Study site

Rhonegletscher is a temperate valley glacier with a length of 9 km and an area of about 16 km² in 2007 (Fig. 1a; Bauder and others, 2007). Having retreated 1700 m from 1878 to 2000, the glacier terminus is now at the top of a steep cliff (Sugiyama and others, 2007). Because the current terminus is located over a depression in the bedrock, a new proglacial lake formed in 2005. The impact of this lake on the glacier is drawing intense glaciological and public attention. The terminus of the glacier is thinning at an increasing rate (Sugiyama and others, 2008) as a result of rising air



Fig. 1. (a) Map of Rhonegletscher with surface contour lines at 100 m intervals. The location of the automatic weather station (AWS) is indicated by a cross. (b) The study site indicated by the box in (a). The locations of ablation stakes are indicated by filled circles. The contour lines show surface elevation at intervals of 20 m. The two proglacial lakes are indicated by the shaded areas. The coordinates correspond to the official Swiss coordinate system.

temperature, elevated ice-flow speed (Tsutaki and others, 2011) and rapid ice dissipation by melting and fragmentation into the lake. Our study site is the region extending approximately 1 km upstream of the glacier from the terminus (Fig. 1b).

Surface melt measurements

The surface melt rate was measured by inserting aluminium ablation stakes 2–4 m in length into the glacier (see Fig. 1b for the stake locations). We installed 44 stakes in July 2009 and monitored their lengths above the surface every 1–10 days. The stakes were redrilled before they melted out. The mean melt rate was calculated over the entire study period from 6 July to 6 September 2009. Because of ice surface roughness and tilt of the stakes, the precision of individual

readings was 10–30 mm. Because the reading error accumulates when the stakes were redrilled, the accuracy in the total melt was about 100 mm. The total melt over the study period in the region was >2 m in ice thickness; thus, the error in the mean melt rate was <5%. The readings were converted to water equivalent (w.e.) by assuming the density of ice to be 900 kg m⁻³.

Albedo measurements

The surface albedo was measured between 1100 and 1600 h on 5 August 2009 in the vicinity of the ablation stakes. The cloud cover on that day was <10% according to visual observation. The upward and downward radiation energies were measured with an albedo meter (EKO Instruments MR-21) and recorded with a datalogger (Hioki 3645). The albedo meter was held 1 m from the ice surface, and the radiation was measured for at least 1 min. The albedo was computed from the radiation energies and incident angle of the solar radiation following the standard procedure (Jonsell and others, 2003; Dewalle and Rango, 2008). The fluctuation in the radiation energies during the 1 min measurement period was <5% (1–2% in general), and the standard deviation in the downward radiation energy over the entire survey period was 4.5%.

Meteorological observations

Meteorological observations were carried out on the western flank of the glacier at 2531 m a.s.l. (Fig. 1a) using an automatic weather station (Vaisala WXT510), installed at a height of 1.8 m from a rock surface, that measured air temperature, precipitation, humidity and wind speed. Sensors measured these variables at 10 s intervals; mean values were recorded every 5 min with a datalogger (Campbell CR1000).

Melt model

We used the following numerical model to compute twodimensional (2-D) snow and ice melt-rate (M (m w.e. d⁻¹)) distributions over the study period on a regular grid of 25×25 m:

$$M = \begin{cases} (f_M + r_{s/i}l)T_m & T_m > 0\\ 0 & T_m \le 0 \end{cases},$$
 (1)

where f_M is a melt factor (m w.e. $d^{-1} \circ C^{-1}$), r_s and r_i are radiation factors for snow and ice surfaces (m $^3\,W^{-1}\,d^{-1}\,^\circ$ C^{-1}), *I* is the daily total potential solar radiation (W m⁻²) and $T_{\rm m}$ is daily mean temperature (°C). The temperature at the elevation of the gridcell is calculated from the weather station data using a lapse rate of dT/dz. The snow/ice surface condition is distinguished by monitoring snow depth computed from modelled snowmelt and solid precipitation. The above model is based on the distributed temperatureindex model reported by Hock (1999; see also Huss and others, 2008a). The dependence of radiation efficiency on surface inclination and shading by surrounding topography is quantified by computing I for each gridpoint from the incident angle of solar radiation and a digital elevation model (DEM), as described by Hock (1999). In the case of a conventional degree-day model, the second term in Equation (1) can be neglected and the parameter f_M is called the 'degree-day factor'.

To apply the model to Rhonegletscher, the parameters f_M and $r_{s/i}$ in Equation (1) and dT/dz were calibrated so that



Fig. 2. (a) Daily mean air temperature (curve) and daily precipitation (bars) and (b) daily mean humidity (bold grey) and hourly mean wind speed. Dates are mm/dd.

(1) the mean misfit of computed total melt with the field data was close to zero and (2) the root-mean-square error was minimized. These parameters were assumed to be constant in space and time. We used a DEM constructed by photogrammetrical evaluation of aerial photographs taken in September 2007 (25 m resolution, ± 0.3 m accuracy) (Bauder and others, 2007). Daily mean air temperatures from the above-mentioned weather station were used to drive the computation.

RESULTS

Meteorological data

Meteorological data obtained from 6 July to 6 September 2009 are shown in Figure 2. During the study period, the mean air temperature was 6.9° C, with a standard deviation of 3.51° C, the total precipitation was 261.0 mm and the mean wind speed was 4.0 m s^{-1} . There was a snowfall event during 17-18 July, resulting in a 0.05-0.1 m thick snow cover on the glacier.

Surface melt

Figure 3a shows a map of the mean melt rate for the period 6 July to 6 September 2009. Ablation stake data are listed in Table 1. The mean melt rate over all measurement sites was 56.1 mm w.e. d^{-1} , with a standard deviation of 7.5 mm w.e. d^{-1} . Measurements at the stakes were interpolated in space with cubic spline interpolation to obtain the overall spatial distribution. The 2-D melt pattern shows substantial spatial variation. Over an elevation range of only 100 m, the melt rate varied by a factor of more than two. For example, there is a spot of low melt in the upper reaches of the study area (32.8 mm w.e. d^{-1} at stake 23), and the melt rate is generally smaller in the northeast part of the studied area. The greatest melt was observed near the eastern margin at stake 2 (71.9 mm w.e. d^{-1}). The melt pattern near the terminus is

Table 1. The locations of the ablation stakes, albedos measured on 5 August 2009, measured (M_{meas}) and computed (M_{comp}) melt rates from 6 July to 6 September 2009 and deviation of the computed melt rates from the measurements, ΔM (($M_{comp}/M_{meas} - 1$) × 100%); coordinates correspond to the official Swiss coordinate system

Stake	Easting	Northing	Albedo	$M_{\rm meas}$	$M_{\rm comp}$	ΔM
_	m	m		mm w.e. d^{-1}	mm w.e. d^{-1}	%
1	672538	159402	0.21	58.21	55.27	-5.0
2	672437	159441	0.11	71.93	54.89	-23.7
3	672410	159350	0.14	60.68	54.90	-9.5
5	672544	159324	0.21	59.17	58.61	-0.9
6	672671	159355	0.25	54.07	55.84	3.3
7	672784	159319	0.11	56.18	56.19	0.0
8	672637	159257	0.10	59.44	57.21	-3.8
9	672596	159198	0.17	64.02	58.37	-8.8
10	672546	159149	0.13	54.94	60.34	9.8
11	672382	159141	0.09	55.02	62.50	13.6
12	672311	159171	0.11	45.87	59.65	30.0
13	672335	159144	0.06	60.56	59.97	-1.0
14	672316	159233	0.09	67.43	55.79	-17.3
15	672236	159166	0.08	52.33	56.00	7.0
16	672281	159145	0.06	61.80	59.37	-3.9
17	672418	159248	0.17	60.31	58.85	-2.4
21	672923	159960	0.24	46.74	49.66	6.2
22	672816	159930	0.30	44.27	50.58	14.2
23	672710	159911	0.33	32.81	51.08	55.7
24	672581	159903	0.24	53.27	52.06	-2.3
25	672777	159471	0.22	49.06	53.53	9.1
26	672683	159544	0.27	53.13	54.55	2.7
30	672498	159840	0.13	52.40	53.32	1.8
31	672532	159642	0.16	55.05	55.24	0.4
32	672896	159378	0.09	59.69	53.34	-10.6
33	672459	159564	0.13	64.35	54.55	-15.2
34	672931	159484	0.12	40.73	51.65	26.8
35	673022	159609	0.10	50.01	50.61	1.2
36	672799	159720	0.26	47.90	53.37	11.4
37	672705	159197	0.09	57.70	53.58	-7.1
38	672360	159246	0.13	62.52	56.56	-9.5
39	672503	159248	0.19	62.38	60.15	-3.6
40	672480	159290	0.16	62.71	58.79	-6.3
41	672494	159129	0.10	55.86	60.98	9.2
42	672450	159143	0.12	59.30	62.65	5.6
48	672203	159149	0.11	54.58	53.27	-2.4
53	672483	159213	0.20	46.79	60.37	29.0
54	672428	159200	0.16	62.20	59.61	-4.2
56	672393	159291	0.12	60.82	55.69	-8.4
59	672334	159194	0.13	53.93	57.19	6.1
Т8	672678	159700	0.21	58.50	54.26	-7.3
Т9	672573	159470	0.24	59.23	55.42	-6.4
T10	672486	159343	0.11	53.49	57.63	7.7
T11	672415	159207	0.08	68.59	58.95	-14.1

spatially complex. In general, the melt rate increases downglacier and from the glacier centre to the margins (Fig. 3a).

The spatial pattern of the melt rate was analysed by computing semivariance:

$$\gamma(h) = \frac{1}{N(h)} \sum_{N(h)} \left\{ \mathcal{M}(\mathbf{x}_i) - \mathcal{M}(\mathbf{x}_j) \right\}^2,$$
(2)

where \mathbf{x}_i is the *i*th stake location and *h* is the so-called lagged distance. The sum is taken over $N(h) \equiv \{(i, j) : h - 50 \text{ m} < |\mathbf{x}_i - \mathbf{x}_j| < h + 50 \text{ m}\}$ (e.g.



Fig. 3. (a) Mean daily melt rates from 6 July to 6 September 2009 in mm w.e. d^{-1} . The contour intervals are 2 mm w.e. d^{-1} . The locations of ablation stakes are indicated by circles. (b) Surface albedos measured on 5 August 2009. The contour intervals are 0.02. (c) Semivariance computed for the observed melt rate (o) and albedo (•) variations. The tolerance in the lagged distance is ± 50 m.

Cressie, 1993). The semivariance, $\gamma(h)$, represents the measure of variance between the data separated by the lagged distance. For example, a low $\gamma(h)$ value indicates that a pair of observations are similar to each other when the

distance between the measurement sites is approximately *h*. A plot of semivariance against the lagged distance is referred to as a semivariogram, which demonstrates the similarity between observations as a function of the distance between the data (Fig. 3c). The semivariance is relatively large in the distance range h < 200 m, showing relatively high local variability in the melt rate. Its increase at $h \sim 400$ m indicates that the correlation rapidly decreases at this distance.

Albedo

Figure 3b shows the 2-D distribution of surface albedo measured on 5 August 2009. Individual measurements are listed in Table 1. The albedo clearly decreases from the centre to the margins and down-glacier towards the terminus. The highest albedo, 0.33, was observed in the upper reaches at stake 23. The albedo drops below 0.2 in the area below stakes 2, 5, 8 and 37. The lowest observed value was 0.06, on a debris-covered surface near the terminus at stakes 13 and 16. These albedos on Rhonegletscher are similar to those measured near the terminus of other mountain glaciers. Brock and others (2000) reported a value of approximately 0.1 at the terminus of Haut Glacier d'Arolla, Switzerland, whereas Klok and others (2003) reported approximately 0.2 at Morteratschgletscher, Switzerland. Jonsell and others (2003) measured 0.06 as the lowest albedo in Storglaciären, Sweden, at a sediment-covered site near the margin.

The semivariogram of the albedo shows features different from that of the melt rate (Fig. 3c). The semivariance is small at short lagged distances, indicating that the albedo values are similar when they are compared within a small scale. It progressively increases within the range 0 < h < 300 m, which implies the albedo is spatially uncorrelated in the region beyond 300 m.

Model results

The model was calibrated to reproduce the observations from 6 July to 6 September 2009. The best-fitting parameter values were $f_M = 1.50 \times 10^{-4} \text{ m w.e. } d^{-1} \circ C^{-1}$, $r_s = 1.32 \times 10^{-5} \text{ m}^3 \text{ W}^{-1} d^{-1} \circ C^{-1}$, $r_i = 2.20 \times 10^{-5} \text{ m}^3 \text{ W}^{-1} d^{-1} \circ C^{-1}$ and $dT/dz = -9.0 \times 10^{-3}$ °C m⁻¹. Figure 4 compares the computed melt rates at mesh gridpoints with the data obtained at the ablation stakes (see also Table 1). The mean difference between the measured and computed melt rates was -0.03 mm w.e. d⁻¹, and the root-mean-square error was 6.7 mm w.e. d⁻¹. The computed melt pattern reproduces several important features of the observational data (Fig. 5a): the melt rate increases down-glacier and there is a low-melt region in the northeast part. Nevertheless, the model predicts weaker spatial variations overall, that is, the high and low melt rates are under- and overestimated, respectively. The discrepancy reaches -24% and +56% at stakes 2 and 23, respectively (Fig. 5b; Table 1). Moreover, the calculated melt rate near the terminus increases from north to south, contrary to the observations.

DISCUSSION

Our measurements revealed a complex spatial melt pattern over the terminus of Rhonegletscher. The mean melt rate during the observation period at stake 2 was more than double that at stake 23. The melt rate generally increases down-glacier, but the spatial variations cannot be explained by surface elevation alone. Degree-day factors (DDFs) were



Fig. 4. Total surface melt from 6 July to 6 September 2009 computed using a melt model for all mesh gridpoints (\cdot) and measured in the field at the stakes (+). The length of the vertical lines indicates the difference between the measured and computed melt at the stake locations.

calculated for every ablation stake by linear regression of cumulative melt on the sum of positive degree-days over the entire study period. Measured air temperature was extrapolated to the stake elevation using a lapse rate of 6.5×10^{-3} °C m⁻¹. DDFs vary from 5.2 mm w.e. d⁻¹ °C⁻¹ to 11.2 mm w.e. d⁻¹ °C⁻¹ for stakes 23 and 2, respectively. These values are within the range of previously reported DDFs on ice surfaces (Braithwaite and Zhang, 2000; Hock, 2003), but the extent of the spatial variation is greater than those obtained for other glaciers (Hock, 2003).

One of the reasons for this spatial variation is the surface albedo. The melt rate was small at stake 23 because the albedo was high, as shown in Figure 3a and b. The complex melt pattern near the terminus also corresponds to the albedo pattern. For example, the low albedo at stake T11 and high albedo at stake 53 coincide with large and small melt rates, respectively. The albedo was lower near the glacier margins, consistent with the trend in melt rate, because ice was contaminated by dark particles related to the emergence of basal ice and the surface was covered with more debris. A scatter plot of DDFs versus albedo at each ablation stake demonstrates the important influence of albedo on the melt rate (Fig. 6a). A linear regression of the data yields a relationship between the DDF and albedo, α , of: DDF= $-8.2\alpha + 10.2$, with a correlation coefficient of r = -0.49 and a *p*-value of 0.0006 (the probability of obtaining |r| > 0.49 assuming the true correlation is zero). Below the line connecting stakes 2, 5, 8 and 37, the albedo dropped and the melt rate increased. In this region, the decrease in albedo seems to be related to the presence of crevasses. Meltwater washed away surface particles in the smooth upper reaches, but surface water flow was impeded in the heavily crevassed lower reaches (Fig. 7a). It should also be noted that the crevassed surface traps more solar radiation than a flat surface, which increases net energy absorption in the region (Pfeffer and Bretherton, 1987).

The observed melt pattern cannot be explained with only albedo variations, as implied by the different spatial



Fig. 5. (a) Melt rates (mm w.e. d^{-1}) computed for the period 6 July to 6 September 2009; and (b) relative deviations from the observed values, ($M_{\text{comp}}/M_{\text{meas}} - 1$)× 100%. The locations of ablation stakes are indicated by circles.

statistical features obtained by the semivariance analysis (Fig. 3c). Another important effect is shading by the surrounding topography. A side-wall to the southeast of the glacier terminus shaded the eastern side of the study area for several hours each morning (Fig. 7b). The low-melt-rate region around stakes 34 and 35 coincides with this area of low potential radiation (Fig. 3a). This effect is taken into account by the potential solar radiation term in the model and is clearly recognizable in Figure 8. The reduced melt rate was therefore reproduced by the computed melt pattern, although its magnitude was smaller than the observation. Correlation of the DDF to the absorbed potential radiation ($I(1 - \alpha)$) is more significant (Fig. 6b; r = 0.55 and p = 0.0001) than the correlation of the DDF to the albedo.

The very strong melt observed at stake 2 is difficult to explain. Albedo increased towards the margins, but the melt rate was greater near the western margin than on the other side of the glacier. Seasonal variation in albedo is often important in the ablation area (e.g. Brock and others, 2000), but no significant change in surface conditions was recognized in this region over the study period. The surface



Fig. 6. (a) DDFs and surface albedos and (b) DDFs and absorbed potential solar radiation, $I(1 - \alpha)$, obtained at the ablation stakes. The lines are linear regressions of the data.

I(1-a) (W m⁻²)

was steeply inclined towards the south in the western part of the glacier, but the model, which includes the incident angle of solar radiation, does not produce a similar pattern. We speculate that the increase in melt rate arises from the absorption of longwave radiation emitted by the bare bedrock on the western flank, which has been exposed by the retreat of the glacier in this region (Fig. 7c). A similar effect has been observed at Franz Josef Glacier, New Zealand (Ishikawa and others, 1992).

Comparing the field data to the computed results confirms the ability of the distributed temperature-index model to include the effects of potential solar radiation. However, several important features in the spatial melt distribution were insufficiently captured. It is clear from the observation at stake 23, for example, that variations in ice albedo are one of the most influential factors not included in the model. Albedo can be included as an additional model parameter (e.g. Pellicciotti and others, 2005); however, our measurements show that its spatial variation is large and



Fig. 7. Photographs showing (a) the lower part of the study area from the southeast, (b) the upper part of the study area from the south and (c) the western margin of the glacier from the southwest. The approximate locations of the ablation stakes are indicated. The photographs were taken on (a) 16 July 2009, (b) 16 July 2009 at 0844 h and (c) 26 July 2008.

does not follow a predictable pattern (Fig. 3b). This implies that albedo would have to be measured over the glacier, which is often not feasible. To compute an accurate estimate of total meltwater production in a region, simple temperature-index models should not be calibrated on singleablation-stake data; the data may be influenced by high small-scale variations in melt rate, as demonstrated by our measurements.



Fig. 8. Potential solar radiation computed for 29 July 2009 (W m⁻²). The contour intervals are 5 W m⁻².

CONCLUSION

We measured glacier surface melt in the terminus of Rhonegletscher at a resolution of 20-100 m. The surface melt rate obtained at 44 stakes over the summer of 2009 showed significant spatial variability. The DDFs obtained from the measured melt at the stakes over a 2 month period ranged from 5.2 to 11.2 mm w.e. d⁻¹ °C⁻¹ within an area extending 1 km from the glacier terminus. Part of the variation can be plausibly explained by differences in surface albedo. Our measurements of albedo range from 0.06 to 0.33, and the highest albedo coincided with low melt rate. The albedo generally decreased from the glacier centre to the margins, in agreement with the observed melt rate variations. The influence of shading by surrounding topography is evident from the field data. The melt rate decreased in the northeast part of the study site, where the potential solar radiation was smaller due to shading by mountain ridges to the east of the glacier. However, some features of the 2-D melt pattern are still difficult to explain. The greatest melt rate was observed near the western margin. Radiation from rock walls close to the glacier is a possible source of the heat energy.

We computed melt rates over the glacier surface using a distributed temperature-index melt model. The model was calibrated using the field data, and the computed spatial melt pattern was compared to observations. The model successfully reproduced the decrease in melt rate due to the shading. Geometrical effects can therefore be taken into account by the model. The model results deviate from the observations by +56% and -24% at the lowest and highest melt rates, respectively. Care should therefore be taken when using such models to investigate a spatial melt pattern at high resolution. Model calibration should be carried out with data sampled in a wide range of ice-surface albedo and other conditions in order to obtain accurate total melt.

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